

1 Binary Trees

- 1.1 Define a procedure, `height`, which takes in a `Node` and outputs the height of the tree. Recall that the height of a leaf node is 0.

```
private int height(Node node) {
```

```
}
```

What is the runtime of `height`?

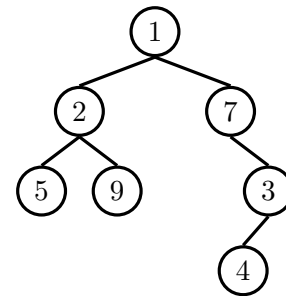
- 1.2 Define a procedure, `isBalanced`, which takes a `Node` and outputs whether or not the tree is balanced. A tree is **balanced** if the left and right branches differ in height by at most one and are themselves balanced.

```
private boolean isBalanced(Node node) {
```

```
}
```

What is the runtime of `isBalanced`?

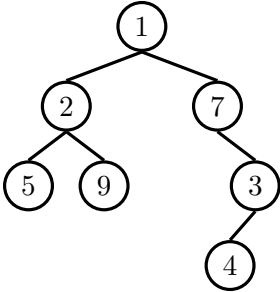
```
public class BinaryTree<T> {  
    protected Node root;  
    protected class Node {  
        public T value;  
        public Node left;  
        public Node right;  
    }  
}
```



2 Traversals

Level-Order Traversals Nodes are visited top-to-bottom, left-to-right.

Depth-First Traversals Visit deep nodes before shallow ones.



2.1 Give the ordering for each depth-first traversal of the tree.

(a) Pre-order

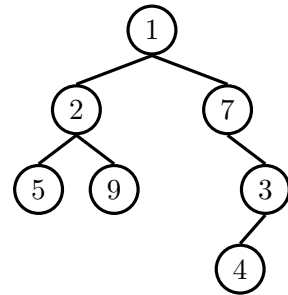
(b) In-order

(c) Post-order

2.2 Give the level-order traversal of the tree.

```

2.3 public void treeTraversal(Fringe<Node> fringe) {
    fringe.add(root);
    while (!fringe.isEmpty()) {
        Node node = fringe.remove();
        System.out.print(node.value);
        if (node.left != null) {
            fringe.add(node.left);
        }
        if (node.right != null) {
            fringe.add(node.right);
        }
    }
}
  
```



What would Java display?

(a) `tree.traversal(new Queue<Node>());`

(b) `tree.traversal(new Stack<Node>());`

3 Binary Search Trees

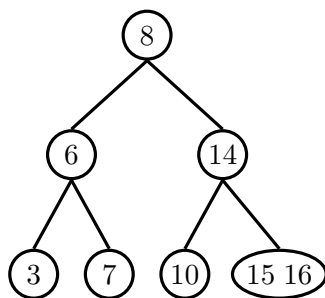
- 3.1 Implement `fromSortedArray` for binary search trees. Given a sorted `int[]` array, efficiently construct a balanced binary search tree containing every element of the array.

```

public class BinarySearchTree<T extends Comparable<T>> {
    protected Node root;
    protected class Node {
        public T value;
        public Node left;
        public Node right;
    }
    public static BinarySearchTree<Integer> fromSortedArray(int[] values) {
        BinarySearchTree<Integer> bst = new BinarySearchTree<>();
        bst.root = bst.fromSortedArray(values, 0, values.length - 1);
        return bst;
    }
    private Node fromSortedArray(int[] values, int lower, int upper) {

```

4 2-3 Forever



4.1 Draw what the 2-3 tree would look like after inserting 18, 12, and 13.

4.2 Now, convert the resulting 2-3 tree to a left-leaning red-black tree.