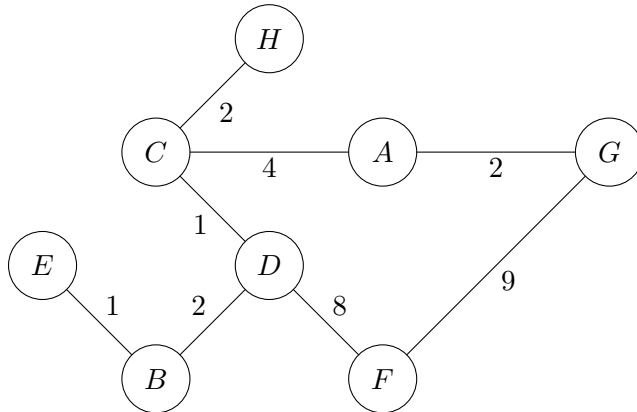


## 1 Searches

- 1.1 For the graph below, write the order in which vertices are visited using the specified algorithm starting from  $A$ . Break ties by alphabetical order. Notice that we have now introduced edge weights to the graph.

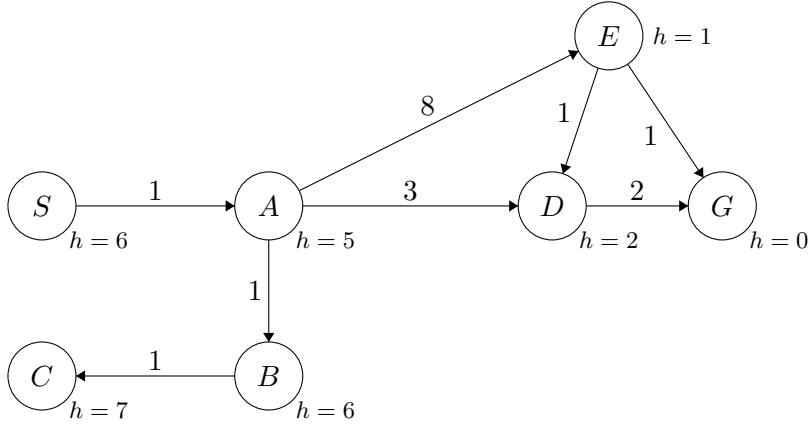


- (a) DFS
- (b) BFS
- (c) Dijkstra's

## 2 Shortest Paths

- 2.1 Find the path from the start,  $S$ , to the goal,  $G$ , when running each of the following algorithms.

The **heuristic**,  $h$ , estimates the distance from each node to the goal.



- (a) Which path does Dijkstra's return?

- (b) Which path does A\* search return?

**A\* search** is an algorithm that combines the total distance from the start with the heuristic to optimize the search procedure.

- (c) What is the runtime of Dijkstra's? A\*? What is the space requirement for both?

### 3 True and False

- 3.1 State if the following statements are True or False, and justify. For all graphs, assume that edge weights are positive and distinct, unless otherwise stated.
- (a) Adding some positive constant  $k$  to every edge weight does not change the shortest path tree from vertex  $S$ .
  
  - (b) Doubling every edge weight does not change the shortest path tree.
  
  - (c) If the weight of each edge is decreased by 1, then the resulting shortest path in any graph from  $u$  to  $v$  is unchanged.
  
  - (d) If an edge  $e$  is the lightest edge connected to vertex  $S$ , it must be a part of the shortest path tree from vertex  $S$ .
  
  - (e) Consider a graph  $G$ , where every edge is nonnegative, except the edges adjacent to vertex  $s$ . Dijkstra's usually fails on graphs with negative edge weights, however if we run Dijkstra's starting from  $s$ , we will get the correct shortest paths tree.