

MORE SCHEME AND INTERPRETERS

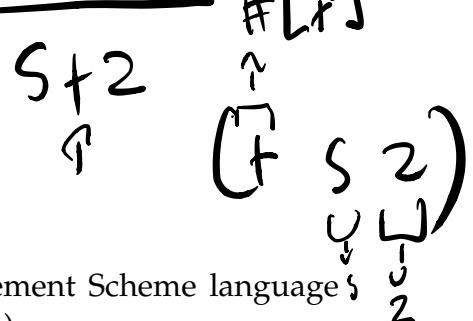
COMPUTER SCIENCE MENTORS

November 9, 2020 - November 12, 2020

Call expressions follow *prefix* notation, i.e. (<operand1> <operand2>
... <operandN>)

Evaluating a call expression closely mirrors Python:

- Evaluate the operator, yielding a procedure p
- Evaluate each operand, each yielding a value argi
- Apply the procedure p with arguments arg1, arg2, ..., argN



Special forms *look* like call expressions but aren't – they implement Scheme language's features and follow special evaluation rules (e.g., short-circuiting).

(Aside: Note that you're free to use a special form name as a variable name, but the name will be looked up *only* in a non-operator position; when used as an operator, it will always refer to the original special form.)

Notable Special Forms:

behavior	syntax
variable assignment	(define <variable-name> <value>)
function defining	(define (<function> <op1>...<opN>) <body>)
if / else	(if <condition> <true-expr> <else-expr>)
if / elif / else	(cond (<cond1> <expr1>) ... (else <else-expr>))
and	(and <operand1> ... <operandN>)
or	(or <operand1> ... <operandN>)
quote	(quote <operand1>)
begin	(begin <expr1> <expr2> ... <exprN>)
lambdas	(lambda (<operand1> ... <operandN>) <body>)
let / execute many lines	(let ((<var1> <val1>) ... (<varN> <valN>)) body)

→ (define a 4)
→ a
→ 'a
→ (eval 'a)

1 What Would Scheme Print?

1. What will Scheme output?

```
scm> (if 1 1 (/ 1 0))
```

1

```
Error scm> (if 0 (/ 1 0) 1)
```

Error

```
scm> (and 1 #f (/ 1 0))
```

#f

```
scm> (and 1 2 3)
```

3

```
scm> (or #f #f #f #f (/ 1 0))
```

0

```
scm> (and (and) (or))
```

#f

```
scm> (define a 4)
```

a

```
scm> ((lambda (x y) (+ a x y)) 1 2)
```

7

```
scm> ((lambda (x y z) (y x z)) 2 / 2)
```

1

```
scm> ((lambda (x) (x x)) (lambda (y) y))
```

y

4

(L₁ L₂)

4

→ (L₂ L₂)

def L₂(y); func argument
return 4

→ 1/0 => zero Division Error

((lambda (y) y) 3)

#t

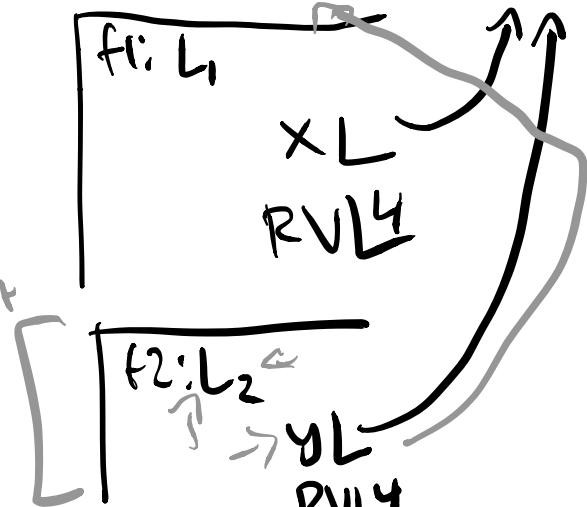
(and) => #t

(or) => #f

↓
↓
y

(1 2 2) => 1

L₁ L → λ(x)
→ L₂ L → λ(y)



2. What will Scheme output?

scm> (define boom1 (/ 1 0))
Error

$$x = \frac{1+1}{1} \times 2$$

scm> (define boom2 (lambda () (/ 1 0)))

boom2

scm> (boom2)

Error

boom1 = 1/0; (a) Why/How are the two boom definitions above different?

boom2 = boom1: sets = to value (1/0)

lambda: 1/0; boom2: sets = to function $\lambda() \Rightarrow (1/0)$

(b) How can we rewrite boom2 without using the lambda operator?

c = 2

(define (boom2) (1/0))

3. What will Scheme output?

scm> (define c 2)

c

scm> (eval 'c)

2

scm> '(cons 1 nil)

(cons 1 nil)

scm> (eval '(cons 1 nil))

(1)

scm> (eval (list 'if '(even? c) 1 2))

// foo =
def foo():
return 1/0

scm> (cons 1 nil)

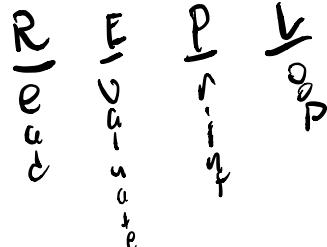
(eval (if (even? c) 1 2))

1

Interpreters

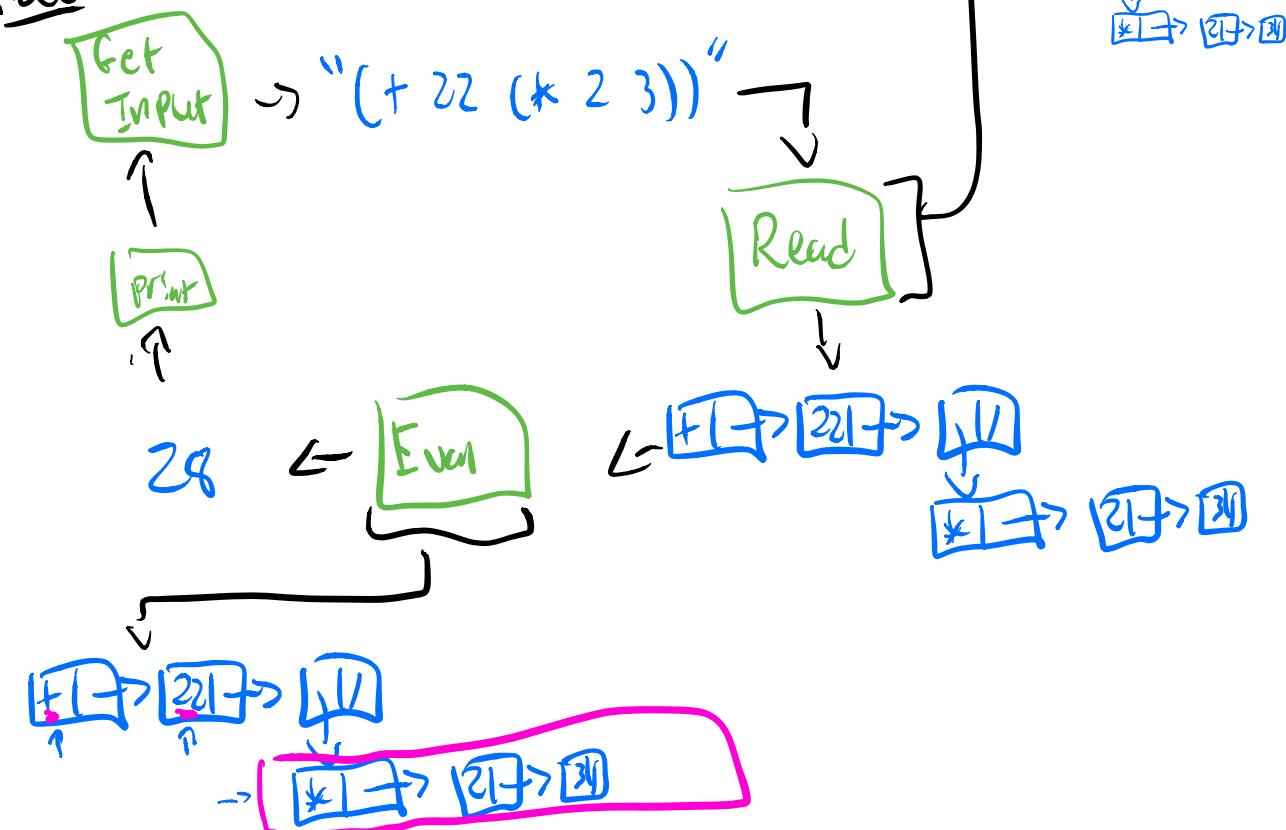
Goal: write a Python program
that can understand / interpret Scheme code

How it's done:



e.g. SCM> (+ 22 (* 2 3))
28
SCM>

Process



Operator: func add, *[+], apply
Operands: [22, 6] → 28
- Can call eval

2 Interpreters

The following questions refer to the Scheme interpreter. Assume we're using the implementation seen in lecture and in the Scheme project.

- What's the purpose of the read stage in a Read-Eval-Print Loop? For our Scheme interpreter, what does it take in, and what does it return?

- 'in' string
- out: linked list (Pair)

- What are the two components of the read stage? What do they do?

1. Lex: gets each individual token from input string

2. Parser: turns tokens \Rightarrow data structure (Pair)

- Write out the constructor for the Pair object the read stage creates with the input string

```
(define (foo x) (+ x 1))
```

Pair(first, Pair(...
 Pair("define", Pair(Pair("foo", Pair("x")), Pair(Pair("+", Pair("x", Pair(1))))))), .first, .second)

- For the previous example, imagine we saved that Pair object to the variable p. How could we check that the expression is a define special form? How would we access the name of the function and the body of the function?

Check (for p)

- p.first == "define"
- name: p.second.first.first
- body: p.second.second.first

5. Circle or write the number of calls to scheme_eval and scheme_apply for the code below.

~~(if 1 (+ 2 3) (/ 1 0))~~

scheme_eval 1 3 4 6

scheme_apply 1 2 3 4

(t 23) => 5

4 => 4

#(t)

don't eval

special forms!

- define
- or, if, etc,

→ def square(x):

→ return x * x

~~(define (square x) (* x x))~~

~~(+ (square 3) (- 3 2))~~

scheme_eval 2 5 14 24

scheme_apply 1 2 3 4

→ eval: 14 → 13 ✓

→ apply: 2 → 3 ✓

~~(define (add x y) (+ x y))~~

~~(add (- 5 3) (or 0 2))~~

3 Code Writing

1. Define **is-prefix**, which takes in a list **p** and a list **lst** and determines if **p** is a prefix of **lst**. That is, it determines if **lst** starts with all the elements in **p**.

; Doctests:

```
→ scm> (is-prefix '() '())
#t
→ scm> (is-prefix '() '(1 2))
#t
scm> (is-prefix '(1) '(1 2))
#t
scm> (is-prefix '(2) '(1 2))
#f
; Note here p is longer than lst
→ scm> (is-prefix '(1 2) '(1))
#f
```

(define (is-prefix p lst)

(cond
 ((null? p) #t)
 ((null? lst) #f))

(else (if (= (car p) (car lst))
 (is-prefix (cdr p) (cdr lst)))
 #f))

)

(and (= (car p) (car lst)) (is-prefix ...)))

)

2. Define **apply-multiple** which takes in a single argument function f , a nonnegative integer n , and a value x and returns the result of applying f to x a total of n times.

; doctests

```
scm> (apply-multiple (lambda (x) (* x x)) 3 2)
256
scm> (apply-multiple (lambda (x) (+ x 1)) 10 1)
11
scm> (apply-multiple (lambda (x) (* 1000 x)) 0 5)
5
```

```
(define (apply-multiple f n x)
```

```
)
```

3. Finish the functions **max** and **max-depth**. **max** takes in two numbers and returns the larger. Function **max-depth** takes in a list **lst** and returns the maximum depth of the list. In a nested scheme list, we define the depth as the number of scheme lists a sublist is nested within. A scheme list with no nested lists has a **max-depth** of 0.

```
; doctests
scm> (max 1 5)
5
scm> (max-depth '(1 2 3))
0
scm> (max-depth '(1 2 (3 (4) 5)))
2
scm> (max-depth '(0 (1 (2 (3 (4) 5) 6) 7)))
4

(define (max x y) _____)

(define (max-depth lst)
  (define (helper lst curr)
    (cond
      ((_____) _____)
      ((_____) (max _____
                    _____)))
      (else (helper _____)))
    )
  )
  (_____)
)
```