EFFICIENCY, LINKED LISTS, AND MIDTERM REVIEW

COMPUTER SCIENCE MENTORS

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1 Efficiency

An order of growth (OOG) characterizes the runtime **efficiency** of a program as its input becomes extremely large. Common runtimes, in increasing order of time, are: constant, logarithmic, linear, quadratic, and exponential.

Examples:

Constant time means that no matter the size of the input, the runtime of your program is consistent. In the function f below, no matter what you pass in for n, the runtime is the same.

```
def f(n):
    return 1 + 2
```

A common example of a linear OOG involves a single for/while loop. In the example below, as n gets larger, the amount of time to run the function grows proportionally.

```
def f(n):
    while n > 0:
        print(n)
        n -= 1
```

An example of a quadratic runtime involves nested for loops. If you increment the value of n by only 1, an additional n amount of work is being done, since the inner for loop will run one more time. This means that the runtime is proportional to n^2 .

```
def f(n):
    for i in range(n):
```

COMPUTER SCIENCE MENTORS 8: EFFICIENCY, LINKED LISTS, AND MIDTERM REVIEW

```
for j in range(n):
    print(i*j)
```

- 1. What is the order of growth for $f \circ \circ$?
 - (a) def foo(n):

for i in range(n):
 print('hello')

(b) What's the order of growth of foo if we change range (n):

- i. To range (n/2)?
 ii. To range (n**2 + 5)?
 iii. To range (10000000)?
- 2. What is the order of growth for belgian_waffle?

```
def belgian_waffle(n):
    total = 0
    while n > 0:
        total += 1
        n = n // 2
    return total
```

2 Linked Lists

Linked lists consists of a series of links which have two attributes: first and rest. First contains some sort of value that is usually what you want to end up storing in the list (these can be integers, strings, lists etc.). Rest, on the other hand, needs to be a pointer to another link or Link.empty, which is just an empty linked list represented traditionally by an empty tuple (but it does not have to be so you should never assume that it is represented by an empty tuple otherwise you may break an abstraction barrier!).

Because each link contains another link or Link.empty, linked lists lend themselves to recursion (just like trees). Consider the following example, in which we double every value in linked list. We mutate the current link and then recursively double the rest.

However, unlike with trees, we can also solve many Linked List questions using iteration with a while loop as well. Take the following example where we have written double_values using a while loop instead of using recursion:

For each of the following problems, assume linked lists are defined as follows:

```
class Link:
    empty = ()
    def __init__(self, first, rest=empty):
        assert rest is Link.empty or isinstance (rest, Link)
        self.first = first
        self.rest = rest
    def __repr__(self):
        if self.rest is not Link.empty:
            rest_repr = ', ' + repr(self.rest)
        else:
            rest_repr = ''
        return 'Link(' + repr(self.first) + rest_repr + ')'
    def __str__(self):
        string = '<'
        while self.rest is not Link.empty:
            string += str(self.first) + ' '
            self = self.rest
        return string + str(self.first) + '>'
```

To check if a Link is empty, compare it against the class attribute Link.empty:

```
if link is Link.empty:
    print('This linked list is empty!')
```

```
1. What will Python output? Draw box-and-pointer diagrams to help determine this.
>>> a = Link(1, Link(2, Link(3)))
>>> a.first
>>> a.first = 5
>>> a.first
>>> a.first
>>> a.rest.first
>>> a.rest.rest.rest.rest.first
>>> a.rest.rest.rest.rest.first
```

>>> repr(Link(1, Link(2, Link(3, Link.empty))))

>>> Link(1, Link(2, Link(3, Link.empty)))

>>> **str**(Link(1, Link(2, Link(3))))

>>> **print**(Link(Link(1), Link(2, Link(3))))

2. Write a function skip, which takes in a Link and returns a new Link with every other element skipped.

```
def skip(lst):
    """
    >>> a = Link(1, Link(2, Link(3, Link(4))))
    >>> a
    Link(1, Link(2, Link(3, Link(4))))
    >>> b = skip(a)
    >>> b
    Link(1, Link(3))
    >>> a
    Link(1, Link(2, Link(3, Link(4)))) # Original is unchanged
    """
    if ______:
    elif ______:
```

3. Now write function skip by mutating the original list, instead of returning a new list. Do NOT call the Link constructor.

```
def skip(lst):
    """
    >>> a = Link(1, Link(2, Link(3, Link(4))))
    >>> skip(a)
    >>> a
    Link(1, Link(3))
    """
```

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4. (Optional) Write has_cycle which takes in a Link and returns True if and only if there is a cycle in the Link.

```
def has_cycle(s):
    """
    >>> has_cycle(Link.empty)
    False
    >>> a = Link(1, Link(2, Link(3)))
    >>> has_cycle(a)
    False
    >>> a.rest.rest.rest = a
    >>> has_cycle(a)
    True
    """
```

3 Midterm Review

1. Draw the box-and-pointer diagram.

```
>>> violet = [7, 77, 17]
>>> violet.append([violet.pop(1)])
>>> dash = violet * 2
>>> jack = dash[3:5]
>>> jackjack = jack.extend(jack)
>>> helen = list(violet)
>>> helen += [jackjack]
>>> helen[2].append(violet)
```

2. Implement subsets, which takes in a list of values and an integer n and returns all subsets of the list of size exactly n in any order. You may not need to use all the lines provided.

```
def subsets(lst, n):
   .....
   >>> three_subsets = subsets(list(range(5)), 3)
   >>> for subset in sorted(three subsets):
          print(subset)
   . . .
   [0, 1, 2]
   [0, 1, 3]
   [0, 1, 4]
   [0, 2, 3]
   [0, 2, 4]
   [0, 3, 4]
   [1, 2, 3]
   [1, 2, 4]
   [1, 3, 4]
   [2, 3, 4]
   .....
   if n == 0:
   if _____:
   return _____
```

COMPUTER SCIENCE MENTORS 8: EFFICIENCY, LINKED LISTS, AND MIDTERM REVIEW

Page 10

3. Write a generator function num_elems that takes in a possibly nested list of numbers lst and yields the number of elements in each nested list before finally yielding the total number of elements (including the elements of nested lists) in lst. For a nested list, yield the size of the inner list before the outer, and if you have multiple nested lists, yield their sizes from left to right.

11000,	yiera	then bizet		,,						
def	num_ """	_elems(l	st):							
	>>> [4]	<pre>>>> list(num_elems([3, [4]</pre>				1]))				
	>>> [2,	list(nu 4, 5, 8	m_elems([1,]	3,	5,	[1,	[3,	5,	[5,	7]]])))
	cour	nt =		_						
	for					:				
		if				:				
		for								_:
			yield							
		else:								
	yie	 ld								

COMPUTER SCIENCE MENTORS 8: EFFICIENCY, LINKED LISTS, AND MIDTERM REVIEW

4. Define delete_path_duplicates, which takes in t, a tree with non-negative labels. If there are any duplicate labels on any path from root to leaf, the function should mutate the label of the occurrences deeper in the tree (i.e. farther from the root) to be the value -1.

Page 11

```
def delete_path_duplicates(t):
  .....
  >>> t = Tree(1, [Tree(2, [Tree(1), Tree(1)])])
  >>> delete_path_duplicates(t)
  >>> t
  Tree(1, [Tree(2, [Tree(-1), Tree(-1)])])
  >>> t2 = Tree(1, [Tree(2), Tree(2, [Tree(2, [Tree(1, Tree
     (5))])])
  >>> delete_path_duplicates(t2)
  >>> t.2
  Tree(1, [Tree(2), Tree(2, [Tree(-1, [Tree(-1, [Tree(5)])])
     1)])
  .....
   def helper(______, _____):
       if _____:
       else:
       for _____ in _____:
```

5. Write a function that returns true only if there exists a path from root to leaf that contains at least n instances of elem in a tree t.

```
def contains_n(elem, n, t):
   .....
   >>> t1 = Tree(1, [Tree(1, [Tree(2)])])
   >>> contains_n(1, 2, t1)
   True
   >>> contains n(2, 2, t1)
   False
   >>> contains n(2, 1, t1)
   True
   >>> t2 = Tree(1, [Tree(2), Tree(1, [Tree(1), Tree(2)])])
   >>> contains_n(1, 3, t2)
   True
   >>> contains_n(2, 2, t2) \# Not on a path
   False
   .....
   if n == 0:
      return True
   elif :
      return
   elif _____:
      return _____
   else:
      return _____
```